

## Factoring Polynomials

- 1) GCF
- 2) Difference of 2 Squares
- 3) Basic trinomial ( $a=1$ )
- 4) Split the Middle ( $a \neq 1$ )
- 5) Grouping (4 terms)

6) Factoring in Quadratic Form:

a)  $x^{\textcircled{8}} - 2x^{\textcircled{4}} - 24$     " $x^{\textcircled{2}} - 2x^{\textcircled{1}} - 24$ "

A                          M

$(x^4 - 6)(x^4 + 4)$

$-6x^4$

$+4x^4$

b)  $\sqrt{16x^4 - 81}$  DOTS  
 (conjugate pairs)  
 $(4x^2 + 9)(4x^2 - 9)$  DOTS

$(4x^2 + 9)(2x + 3)(2x - 3)$

c)  $3p^8 + 15p^5 + 18p^2$   
 $\frac{GCF}{3p^2} (p^6 + 5p^3 + 6)$   
 $3p^2 (p^3 + 3)(p^3 + 2)$

1) Sum + Difference of  
Perfect Cubes:

$$\sqrt[3]{a^3} + \sqrt[3]{b^3} = (a+b) (a^2 - a \cdot b + b^2)$$

S
O
AP

$$a^3 - b^3 = (a-b) (a^2 + a \cdot b + b^2)$$

S
O
AP

"SOAP": Same, Opposite,  
Always Positive

$$a) \sqrt[3]{x^3} + \sqrt[3]{1} = \underbrace{(x+1)}_S \underbrace{(x^2 - 1x + 1)}_{\substack{O \\ AP}}$$

$$b) \sqrt[3]{27x^3} - \sqrt[3]{8} = \underbrace{(3x-2)}_S \underbrace{((3x)^2 + (3x \cdot 2) + 2^2)}_{\substack{O \\ AP}}$$

$$c) \sqrt[3]{x^3} - \sqrt[3]{125} = \boxed{(3x-2)(9x^2+6x+4)}$$

$$= \boxed{\underbrace{(x-5)}_S \underbrace{(x^2+5x+25)}_{\substack{O \\ AP}}}$$

$$d) 16x^5 + 54x^2$$

\*GCF  
1st

$$2x^2 \sqrt[3]{8x^3} + \sqrt[3]{27}$$

$$\underbrace{(2x+3)}_S \underbrace{((2x)^2 - (2x \cdot 3) + 3^2)}_{\substack{O \\ AP}}$$

$2x^2$	$(2x+3)$	$(4x^2 - 6x + 9)$
$x=0$	$x = -\frac{3}{2}$	$x = ?$